



1/40

NKS Experimental Design and Implementation for Students

Jamie Raymond
Northeastern University
raymond@ccs.neu.edu

An NKS 2004 Presentation



Back

Close



Introduction

- Experimentation is at the heart of NKS.
- Conducting general NKS experiments involves programming.
- Where can NKS and programming meet at the pre-college level?



Back

Close



Pre-college

Two approaches to introducing NKS

1. Computing courses: interesting problem domain
2. Domain courses (science,math):
computer experiments that require programming

My Experience



Back

Close



Roadmap

- NKS Experimental Design
- Programming for NKS Experiments
- TeachScheme!
- Introductory NKS Exercise



Back

Close



NKS Experiments

Simple Programs

- CAs, Turing machines, substitution systems,
- numerical systems, multiway systems, and et cetera.

Experimentation

- Data generation
- Analysis (visual, statistical, etc.)



Back

Close



Scientific Method for NKS

Textbook Scientific Method

1. Observation
2. Hypothesis
3. Experiment
4. Conclusion



Back

Close



Scientific Method for NKS

NKS Scientific Method

1. Observation
2. Question
3. Visualization
4. Experiment: Generation and Analysis
5. Conclusion



Back

Close



Beginning Programmers

Cognitive Model

Issues

- Syntax
- Errors
- Blank screen



Back

Close

Programming

- Language
- Environment
- Methodology



Back

Close



10/40

One language fits all?

- C?
- Java?
- Python?
- Scheme?
- Mathematica?



Back

Close



TeachScheme!

Less syntax, more problem solving

Pillars of TeachScheme!

- Curriculum
- Language Levels
- Programming Environment



Back

Close



Curriculum

- *How to Design Programs*
Felleisen, Findler, Flatt, Krishnamurthi
MIT Press, 2000
- <http://www.htdp.org>



Back

Close



Design Recipe

1. Problem Analysis & Data Definition
2. Contract, Purpose, Header
3. Examples
4. Function Template
5. Function Definition
6. Tests



Back

Close



Template matches Data Definition

A List-of-Number is one of:

```
-- empty  
-- (cons Number List-of-Number)
```

```
;;Template
```

```
;;LON-f: List-of-Number -> ???
```

```
(define (LON-f a-lon)
```

```
  (cond
```

```
    [(empty? a-lon) ...]
```

```
    [(cons? a-lon) ... (first a-lon) ...
```

```
      ... (LON-f (rest a-lon)) ]))
```



Back

Close



15/40

Language Levels

- Beginner through Advanced
- Better error reporting
- More pedagogic control
- Teachpacks



Back

Close



16/40

Programming Environment: DrScheme



Back

Close

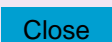
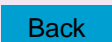
SK.scm - DrScheme

SK.scm
(define ...) Save Step Check Syntax Execute Break

```
|#  
  
;;count-s: SK-exp -> Number  
;; return the number of S in the exp  
(define (count-s ask)  
  (cond  
    [(empty? ask) 0]  
    [(cons? (first ask)) (+ (count-s (first ask))  
                             (count-s (rest ask)))]  
    [(symbol=? (first ask) 'k)  
     (count-s (rest ask))]  
    [(symbol=? (first ask) 's)  
     (+ 1 (count-s (rest ask)))]]))  
  
(count-s empty) "should be" 0  
(count-s '(s)) "should be" 1
```

Welcome to [DrScheme](#), version 206.1-cvs1mar2004.
Language: [Beginning Student with List Abbreviations](#).
>

49:0 GC 43,556,864 Read/Write not running





DrScheme

- Interactive
- Algebraic Stepper
- Syntax Checker
- Errors Matter!



Back

Close



Introductory NKS Exercise

Analyze an arbitrarily complicated S-K combinator expression and produce the the number of Ss in the expression.

Extensions

- Statistics (e.g. distribution of S and K)
- Generation (create raw data)
- Compilation (combinators emulating other systems)



Back

Close



S-K Combinators

- Symbolic system (see NKS, pg 711)

- Two rules:

$$s[x_][y_][z_]\rightarrow x[z][y[z]]$$
$$k[x_][y_]\rightarrow x$$

- $s[s[k[s]][s[k[s[s[k][k]]]]][s[k[k]][s[s[s[s[s[k][k]]]]]]]$



Back

Close



Data Definition

An SK-Exp is one of:

empty

(cons 's SK-Exp)

(cons 'k SK-Exp)

(cons SK-Exp SK-Exp)



Back

Close



Contract/Purpose/Header

```
;;count-s: SK-exp -> Number  
;; return the number of S in the exp  
(define (count-s ask) ...)
```

[Back](#)[Close](#)



Examples

```
(count-s empty) "should be" 0
```

```
(count-s '(s)) "should be" 1
```

```
(count-s '(s k s)) "should be" 2
```

```
(count-s '((s s k (s (s s k))) k)) "should be" 5
```



Back

Close



Function Template

Reminder: Data Definition

An SK-Exp is one of:

```
empty
(cons 's SK-Exp)
(cons 'k SK-Exp)
(cons SK-Exp SK-Exp)
```

Template

```
(define (SK-fun ask)
  (cond
    [(empty? ask) ...]
    [(cons? (first ask)) ... (SK-fun (first ask))
     ... (SK-fun (rest ask)) ...]
    [(symbol=? (first ask) 's)
     ... (first ask) ... (SK-fun (rest ask)) ...]
    [(symbol=? (first ask) 'k)
     ... (first ask) ... (SK-fun (rest ask)) ...]))
```



Back

Close



Function Body

```
(define (count-s ask)
  (cond
    [(empty? ask) 0]
    [(cons? (first ask))
     (+ (count-s (first ask)) (count-s (rest ask)))]
    [(symbol=? (first ask) 'k) (count-s (rest ask))]
    [(symbol=? (first ask) 's)
     (+ 1 (count-s (rest ask)))]))
```

[Back](#)[Close](#)

Testing



26/40



Back

Close

```
SK.scm - DrScheme
[SK.scm] [define...] Save Step Check Syntax Execute Break
;;count-s: SK-exp -> Number
;; return the number of S in the exp
(define (count-s ask)
  (cond
    [(empty? ask) 0]
    [(cons? (first ask)) (+ (count-s (first ask))
                           (count-s (rest ask)))]
    [(symbol=? (first ask) 'k)
     (count-s (rest ask))]
    [(symbol=? (first ask) 's)
     (+ 1 (count-s (rest ask)))]))

(count-s empty) "should be" 0
(count-s '(s)) "should be" 1
(count-s '(s k s)) "should be" 2
(count-s '((s s k (s (s s k))) k)) "should be" 5

Language: Beginning Student with List Abbreviations.
0
"should be"
0
1
"should be"
1
2
"should be"
2
5
"should be"
5
>
```

15:2

GC

43,556,864

Read/Write

not running





28/40

S-K Combinators: Mathematica



Back

Close



Data Definition

Data Definition

An SK-exp is one of:

```
{}
```

```
Prepend[SK-exp, "s"]
```

```
Prepend[SK-exp, "k"]
```

```
Prepend[SK-exp, SK-exp]
```



Back

Close



Examples

```
SCount [{}] === 0
```

```
SCount [{"S"}] === 1
```

```
SCount [{"S", "K"}] === 1
```

```
SCount [{"S", {"K"}}] === 1
```

```
SCount [{"S", "S", "K", {"S", {"S", "S", "K"}}}, "K"]  
=== 5
```



Back

Close



Body

```
Clear[SCount];  
SCount[ske_] :=  
  Which[  
    ske == {}, 0,  
    First[ske] === "S", 1 + SCount[Rest[ske]],  
    First[ske] === "K", SCount[Rest[ske]],  
    True, SCount[First[ske]] + SCount[Rest[ske]]];
```



Back

Close

Testing



32/40



Back

Close

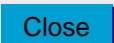


```
Presentation.nb -STUDENT VERSION-

In[1]:= Clear[SKCount];
SKCount[ske_] :=
  Which[
    ske == {}, 0,
    First[ske] == "S", 1 + SKCount[Rest[ske]],
    First[ske] == "K", 1 + SKCount[Rest[ske]],
    True, SKCount[First[ske]] + SKCount[Rest[ske]]];
SKCount[{}] == 0
SKCount[{"S"}] == 1
SKCount[{"S", "K"}] == 2
SKCount[{"S", {"K"}}] == 2
SKCount[
  {"S", "S", "K", {"S", {"S", "S", "K"}},
  "K"}] == 8

Out[3]= True
Out[4]= True
Out[5]= True
Out[6]= True
Out[7]= True

200%
```



Errors



34/40



Back

Close



35/40

```
SK.scm - DrScheme
[SK.scm] Save Step Check Syntax Execute Break
Check Syntax function call: expected a defined name or a
Error Message primitive operation name after an open
Hide

[(eq? (first ask) 'k) ...(first ask)...
      ...(SK-fun (rest ask))...]])
|#

;;count-s: SK-exp -> Number
;; return the number of S in the exp
(define (count-s ask)
  (cond
    [(empty? ask) 0]
    [(cons? (first ask)) ((+ (count-s (first ask))
                             (count-s (rest ask)))]
    [(symbol=? (first ask) 'k)
     (count-s (rest ask))]
    [(symbol=? (first ask) 's)
     (+ 1 (count-s (rest ask)))]])

;(count-s empty) "should be" 0
(count-s '(s)) "should be" 1
(count-s '(s k s)) "should be" 2
(count-s '((s s k (s (s s k))) k)) "should be" 5

37:26 GC 43,556,864 Read/Write not running
```



Back

Close



SK.scm - DrScheme

Step Check Syntax Execute Break

```
(define (count-s ask)
  (cond
    [(empty? ask) 0]
    [(cons? (first ask)) (+ (count-s (first ask))
                           (count-s (rest ask)))]
    [(symbol=? (first ask) 'k)
     (count-s (rest ask))]
    [(symbol=? (first ask) 's)
     (+ 1 (count-s (rest ask)))]))

(count-s empty) "should be" 0
(count-s '(s)) "should be" 1
(count-s '(s k s)) "should be" 2
(count-s '((s s k (s (s s k))) k)) "should be" 5
(count-s 1 2 3)
```

Welcome to [DrScheme](#), version 206.1-cvs1mar2004.
Language: [Beginning Student with List Abbreviations](#).
count-s: this procedure expects 1 argument, here it is provided 3 arguments
>

49:0 GC 43,556,864 Read/Write not running



Back

Close

Stepper



37/40



Back

Close

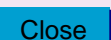


```
Stepper
Home |< Application < Step > Step > Application >|

(define (count-s ask)
  (cond
    ((empty? ask) 0)
    ((cons? (first ask))
     (+ (count-s (first ask)) (count-s (rest ask))))
    ((symbol=? (first ask) 'k) (count-s (rest ask)))
    ((symbol=? (first ask) 's) (+ 1 (count-s (rest ask))))))

(count-s (list 's))
```

```
(cond
  ((empty? (list 's)) 0)
  ((cons? (first (list 's)))
   (+
    (count-s
     (first (list 's)))
    (count-s
     (rest (list 's)))))
  ((symbol=?
   (first (list 's))
   'k)
   (count-s
    (rest (list 's))))
  ((symbol=?
   (first (list 's))
   's)
   (+
    1
    (count-s
     (rest (list 's)))))
```





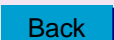
Stepper

Home |< Application < Step Step > Application >|

```
(define (count-s ask)
  (cond
    ((empty? ask) 0)
    ((cons? (first ask))
     (+ (count-s (first ask)) (count-s (rest ask))))
    ((symbol=? (first ask) 'k) (count-s (rest ask)))
    ((symbol=? (first ask) 's) (+ 1 (count-s (rest ask))))))

(cond
  ((empty? (list 's)) 0)
  ((cons? (first (list 's)))
   (+
    (count-s
     (first (list 's)))
    (count-s
     (rest (list 's)))))
  ((symbol=?
    (first (list 's))
    'k)
   (count-s
    (rest (list 's))))
  ((symbol=?
    (first (list 's))
    's)
   (+
    1
    (count-s
     (rest (list 's))))))

(cond
  (false 0)
  ((cons? (first (list 's)))
   (+
    (count-s
     (first (list 's)))
    (count-s
     (rest (list 's)))))
  ((symbol=?
    (first (list 's))
    'k)
   (count-s
    (rest (list 's))))
  ((symbol=?
    (first (list 's))
    's)
   (+
    1
    (count-s
     (rest (list 's))))))
```





Concluding Thoughts

- Programming and NKS
- Little languages
- Future directions

<http://www.ccs.neu.edu/home/raymond/TeachNKS>



Back

Close